

Summary

Generally

$$(2) \quad dI(s) = -\beta_{\text{ext}} ds I(s) + \beta_{\text{abs}} ds B(T(s)) + \beta_{\text{sca}} ds \int_{4\pi} P(\hat{\Omega}', \hat{\Omega}) I(\hat{\Omega}', s) d\omega$$

$$(3) \quad \frac{dI(s)}{\beta_{\text{ext}} ds} = \underbrace{-I(s)}_{\text{Extinction}} + \underbrace{(1-\bar{\omega})B(T(s))}_{\text{Emission}} + \bar{\omega} \int_{4\pi} \underbrace{P(\hat{\Omega}', \hat{\Omega})}_{\text{Scattering}} \underbrace{I(\hat{\Omega}', s)}_{4\pi} d\omega$$

$$\bar{\omega} = \text{Single Scattering Albedo} = \frac{\beta_{\text{sca}}}{\beta_{\text{ext}}} = \frac{\beta_{\text{ext}} - \beta_{\text{abs}}}{\beta_{\text{ext}}}$$

(2) and (3) are the general forms of Equations that describe radiation transfer.

Parameters to Study:

$$\beta_{\text{abs}} = \underbrace{\sum_i \sigma_{\text{abs},i} N_i}_{\substack{\text{Distance}^2 \times \text{\# Things that absorb of type } i \\ \text{Distance}^3}} \quad \left(\frac{1}{\text{distance}} \right)$$

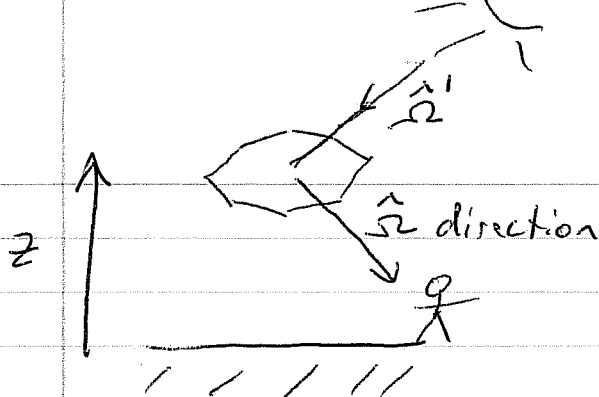
$$\beta_{\text{sca}} = \sum_i \sigma_{\text{sca},i} N_i$$

$$\beta_{\text{ext}} = \beta_{\text{sca}} + \beta_{\text{abs}}$$

$$\bar{\omega} = \frac{\beta_{\text{sca}}}{\beta_{\text{ext}}} \quad \text{Probability that the extinction event results in Scattering}$$

$$P(\hat{\Omega}', \hat{\Omega}) \sim \text{Probability that light scattered by things goes in direction } \hat{\Omega}.$$

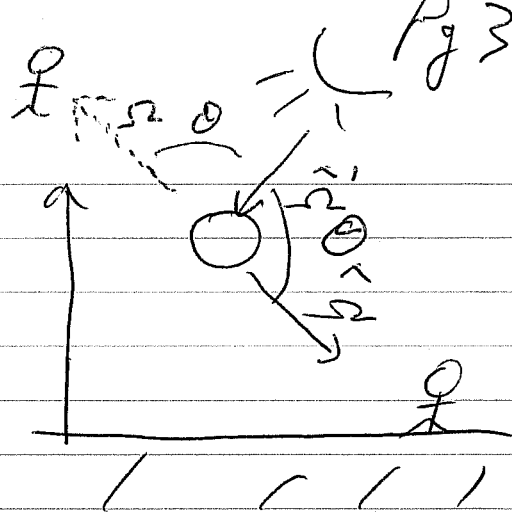
Some thoughts on the Phase function follow.



"Large" oriented crystals:
 Z direction important,
 Use $P(\hat{\Omega}', \hat{\Omega}, \hat{z})$

(Want consider)

(Hydrodynamics
 determines
 orientation)



Spherical Particle or
 Randomly oriented
 Non spherical Particle

"small" ice crystals, aerosol
 Generally only need Θ ,
 $\cos \Theta \equiv \hat{\Omega}' \cdot \hat{\Omega}$

$$P(\hat{\Omega}', \hat{\Omega}) \equiv P(\cos \Theta)$$

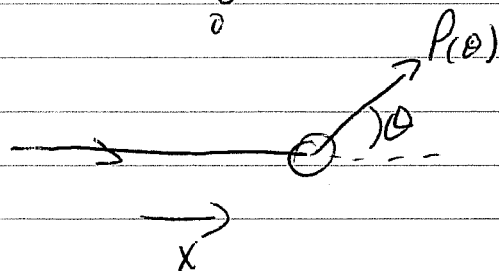
Normalization of the Phase function for spheres or
 randomly oriented nonspherical particles:

$$\frac{1}{4\pi} \int_0^{2\pi} \int_0^\pi P(\cos \Theta) \sin \Theta d\Theta d\phi = 1 \quad \text{or} \quad \text{Do } \phi, \quad \mu \equiv \cos \Theta \quad d\mu = -\sin \Theta d\Theta$$

$$\frac{1}{2} \int_0^\pi P(\cos \Theta) \sin \Theta d\Theta = \frac{1}{2} \int_{-1}^1 P(\mu) d\mu = 1$$

Asymmetry Parameter: g $-1 \leq g \leq 1$

$$g \equiv \frac{1}{2} \int_0^\pi P(\cos \Theta) \cos \Theta \sin \Theta d\Theta = \frac{1}{2} \int_{-1}^1 P(\mu) \mu d\mu$$

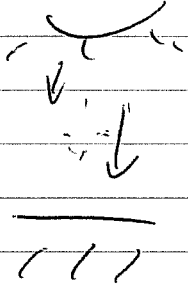


$\cos \Theta$ brings out the
 part of $P(\Theta)$ that
 goes in the original direction
 (+x in this case)

Used
 for
 1-D
 Models

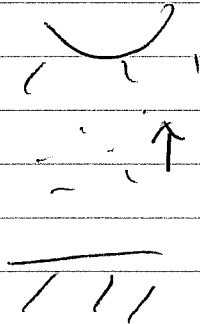
Cases of asymmetry Parameter

$g=1$



All scattered light in the forward direction

$g=-1$



All scattered light in backward direction.

In 1-D, Probability forward Scatter = $\frac{1+g}{2}$
 $-1 \leq g \leq 1$

Backward Scatter = $\frac{1-g}{2}$

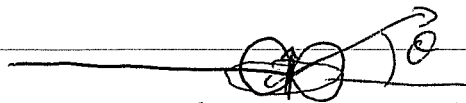
Generally $P(\theta)$ and g must be calculated from Mie theory or appropriate theory. Simple model phase function is

Henyey - Greenstein Phase function:

$$P_{HG}(\cos\theta) = \frac{1 - g^2}{(1 + g^2 - 2g\cos\theta)^{3/2}}$$

Rayleigh Phase function for air molecules in Vis.

$$P_R(\cos\theta) = \frac{3}{4} (1 + \cos^2\theta)$$



Study will be in depth